KINEMATICS OF NONEXTENSIVE STATISTICAL SYSTEMS

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A field theory is developed for nonextensive statistical systems on the basis of the generating functional

$$Z_q\{u(\mathbf{r},t)\} = \int Z_q\{x\} e_q \left[\int ux(Z\{x\})^{q-1} d\mathbf{r} dt \right] Dx$$

Here, $q \in (0, \infty)$ is deformation parameter; $x(\mathbf{r},t)$ and $u(\mathbf{r},t)$ are fluctuating order parameter and its conjugate field, respectively; $e_q(x) := [1+(1-q)x]^{1/1-q}$ is the Tsallis exponential related to $1+(1-q)x \ge 0$. The generating functional represents a generalized Fourier-Laplace transform of the partition functional

$$Z_q \{u(\mathbf{r},t)\} = \frac{2\pi}{2-q} \int e_q \left[-Sx\{x(\mathbf{r},t), p(\mathbf{r},t)\}\right] Dp$$

being integral over generalized momentum $p(\mathbf{r},t)$ conjugated to the generalized coordinate $x(\mathbf{r},t)$. Here, the effective action $S = \int \mathcal{L} dt$ is defined by the Lagrangian

$$\mathcal{L} = p(x - \nabla^2 x + \frac{\partial F}{\partial x}) - \frac{p^2}{2}$$

Equations of the system evolution within phase space is shown to be non-dependent of the deformation parameter, whose value determines only the probability to realize phase trajectories

$$P_q\{x(\boldsymbol{r},t),p(\boldsymbol{r},t)\} \propto e_q[-Sx\{x(\boldsymbol{r},t),p(\boldsymbol{r},t)\}].$$

Within the harmonic approach, deformed partition function and moments of the order parameter of lower powers are found. A set of equations for the generating functional is obtained to take into account constraints and symmetry of the statistical system.