# CRITICAL EXPONENTS IN PERCOLATION MODEL OF TRACK REGIONS WITH DIFFERENT DEPTH DISTRIBUTION

#### Demchyshyn Andriy, Selyshchev Pavlo

Taras Shevchenko National University of Kyiv, Faculty of Physics , 03187, Ukraine, Kyiv

# ABSTRACT

As a result of irradiation with Xe with E = 250 MeV in InP at room temperature [1] defects, similar to the "chain of pearls", which are placed along the trajectory of the ions at depths ranging from 35 to 100 nm and from 7 to 10 microns have been identified. Such defects called tracks, and they can occur at different depths and have different shapes. Tracks were examined like a chain of deal spherical regions; it was assumed that each incident ion creates one such chain. In this model, we assume that the track is formed randomly, but in that place of the ion path, where the energy value, which loses each ion to the unity of the way, is above some threshold value.

As a result of irradiation the number of tracks will continue to grow, areas of the single tracks modified substance continue to overlap, form of modificated matter becomes more complicated, creating branched structure.

Percolation threshold, fraction of spanning cluster modified material for different doses and different distributions of track areas in depth were evaluated. Based on the scaling hypothesis large-scale curve were constructed, critical exponents for this percolation model were established.

Calculated values of critical exponents were compared with the known values for the model of continuous percolation. Parameters of the percolation and critical exponents depend on the distribution of track areas in depth, which indicates the difference in the order parameters of the track structure obtained for different distributions in depth.

**Key words:** track, branched structures, swift heavy ions, the Monte Carlo method, critical exponents, percolation threshold, percolation.

# INTRODUCTION

Under swift heavy ions (SHI) irradiation track of various shapes and lengths, filled with a modified (with respect to the material of the sample) material, are formed in a solid. They are generated as a result of the strong relaxation of electronic excitations and formed along the trajectory of the ion. Tracks are beginning both from the irradiated surface and at some distance from it. Continuous and discontinuous cylindrical and spherical track field were found.

Elongated defects, similar to the "chain of pearls" that are placed along the trajectory of the ions at depths ranging from 35 to 100 nm and from 7 to 10 microns, were found after irradiation by xenon ions with E = 250 MeV in InP at room temperature [1]. Also in the iron garnet irradiated by ions with energies

around 12 MeV in a mode of high speed [2] with the energy loss in the range of 4.5 -7 KeV·nm^(-1) the appearance of spherical domains of the modified material were observed. Discrete tracks point-shaped and oblong dark spots with a diameter equal to an average of about 3 - 10 nm along the trajectories of incoming ions in the form of a "chain of pearls" with a number of "pearls" in the track of two to five pieces were observed on the bright-field pictures in the paper [3].

Physical mechanisms of track formation, probability distribution of their formation along the trajectory and in the chain have not been yet fully clarified. The distribution of the tracks in the depth of the sample did not correlate with either the distribution of implanted ions, or the distribution of point defects formed by the ions. The experimental results do not uniquely determine the distribution of tracks.

However, it is widely recognized that the track is formed as a result of redistribution of the energy transmitted by one ion in the electron subsystem. Also it is known that the track is formed randomly in that place of the ion path, where the value of missing energy per unit of ion path is above a certain threshold, in a place where the rush of energy release is presented. It was noted that the simulation results of energy spectra using the SRIM 2008, shows that the maximum energy during the passage of high-energy ions are also located in an average of 25-40 nm. From the experimental data it is known that the tracks in the form of a chain of spheres are created at different depths (between 0 and 50 nm ,between 0 and 500 nm) for different materials and conditions of exposure. For example, for InP irradiated by xenon ions, the average distance between tracks spherical averages of 25-40 nm, length of the chain is in the range from 50 nm to 150 nm.

Study of changes in material properties as a result of electronic excitation upon irradiation by fast heavy ions and the creation of latent tracks in these materials is an exciting and promising field for new research and development. However, despite the relevance of the topic and practical significance of the expected results, the formation of branched structures of the individual tracks has been insufficiently studied.

# FORMULATION OF THE PROBLEM

We simulated a sample in the form of plane-parallel plate with a thickness of 50 to 300 nm. For the calculations was chosen fragment of the plate in the shape of the box size from 50 to 300 nm. The case where the ion energy is sufficient to create a chain of spheres modified substances, energy is 20-40 MeV / amu around was modeled. Each incident ion creates a track in a sequence of a certain number of spherical regions. The trajectories of all ions are parallel to each other. In this model, we simulate different distribution areas in depth, such as: a) a sphere in the chain b) a sphere in a chain or two areas in the chain) is a sphere or two areas or three areas. And so on up to six spheres in the chain.

The first spherical region is equally likely to appear anywhere in the segment of the trajectory of an ion from its point of penetration into the sample to the point of  $2\rho$ , where  $\rho$  - the average distance between the spheres. In the calculations  $\rho$  is equal to 40 nm. The distance from the first sphere to the second is chosen randomly from range of values between 0 and  $2\rho$ , the form of distribution doesn't depend on the «history» (it is the same as for the preliminary scope, only shifted along the ion path in the appearance point of the previous sphere). Some specific distribution of tracking areas in depth was obtained as a result, distribution for the case when there are maximum three spheres in the chain is shown in *Fig.1*.



Consecutively two surfaces were exposed to radiation.

With the irradiation modified substance areas of individual tracks start to overlap, as a result modified form of matter becomes more complicated,

forming a branched structure. Some part of this branched structure is bordered on one surface of the sample, while others lie on the boundary with the opposite surface. When these parts connect one to another, they will create so-called "spanning cluster," which percolates from one surface to another.



# **RESULTS AND DISCUSSION**

Fig.2. - Dependence of the branched structure surface area on the dose and from different angles

Computed dependence of the branched structure surface area on the dose and from different angles has previously been reported (*Fig.2*).

This nontrivial dependence is related with the distribution of track regions in depth, namely, the correlation between the modified regions of different tracks as a "chain of spheres." Scaling hypothesis has been used to separate influence of this distribution on the angular and dose dependence of structural parameters.

Percolation threshold, fraction of spanning cluster modified material for different doses and different distributions of track areas in depth for different scales of the sample were evaluated. Based on the scaling hypothesis largescale curve were constructed, critical exponents for this percolation model was established.

Scale was changed in the following way: the sample size was increased in two times, irradiation dose – in four times, the number of spheres in the chain in two times (to make modified structure density and percolation effects didn't change).

For each scale dependence of the appearance frequency of first spanning cluster (percolation) on the number of spheres was obtained, in each case deal number of areas, where percolation is most frequent, was defined. This value corresponds to a value of modified material share, which is the percolation threshold for corresponding finite size of sample and will approach the percolation threshold of the infinite cluster. Using the percolation threshold dependence on the number of track regions in the sample the percolation threshold of the infinite cluster.

Differences between the critical exponents of this model and the wellknown model of uniform distributed spherical domains in volume (continuous percolation model) were received.

## CONCLUSIONS

As a result, it was found that the difference critical exponents of this model and the continuous percolation model indicates that the dependence of the modified structure area on the dose and the angle related with the distribution of track regions in the depth of the sample. Also, correlation of individual track regions result in higher ratio of the critical exponents than in a continuous percolation model, that talks about the higher connectivity of track regions structure in this model. Also it causes fact that percolation threshold in this case is below the percolation threshold of continuous percolation. Created model based on experiments and has vivid scaling properties, that allows us to predict different parameters of the modified structure at different scales of the sample.

#### REFERENCES

- [1] Herre O., Wesch W., Wendler E. Phys. Rev. B -1998.-vol. 58 -p.4832.
- [2] Meftah A., Brisard F., Costantini J. M. et al. Physical Review B.- 1993. Vol. 48.
  P. 920 925.
- [3] Gaiduk P.I., Nylandsted Larsen A. et al. Phys. Rev. B., 2002. Vol. 66.— P. 045316-2 - 045316-3.