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### MARKETING OF UKRAINIAN HIGHER EDUCATIONAL INSTITUTIONS REPRESENTATION BASED ON MODELING OF WEBOMETRICS RANKING

Abstract. The objective of the article is constructing of the two-factor model on the basis of the statistical material of the Webometric Rating of Universities, which analytically describes the status of Ukrainian higher educational institutions in terms of Webometrics indicators, provides an opportunity for its quantitative and qualitative analysis and forecasting of development trends of market educational services and marketing research in this area. The statistical analysis of the data of the Webometric Rating of Universities was conducted using the professional statistical information processing program STATGRAPHICS Centurion XV.I. Analytical relations are obtained using the Pade approximation technique. Mathematical editor Maple has been used to visualize the results of research and illustrate a qualitative picture of the rating of Ukrainian universities in the Internet space using the Webometric Indicators system. A two-factor model of the state and forecast of academic representation of Ukrainian universities according to Webometric rating is constructed. Using the proposed model, an analytical expression is obtained that allows for quantitative and qualitative assessments of the world ranking of higher educational institutions of Ukraine in the Webindicators system Webometrix in order to increase their academic presence on the Internet, to strengthen the international authority and raise the national science school as a whole for a qualitatively new degree of development. The scientific novelty of the work is in the inclusion in the model of the time factor, the availability of which makes it possible, firstly, to extend the statistical material used in time and, secondly, to predict the trends and prospects of presentation in the Internet space of Ukrainian universities as advanced research centers. The main results of the work can be useful as a methodological material during the educational process in higher educational institutions, in the training and improvement of the skills of management personnel, in developing programs for reforming the educational process in higher education in order to bring it closer to European requirements and achieve the level of the best world universities. The presented methodology and data analysis algorithm can be generalized to evaluate rating systems of other nature: when evaluating students' educational and community work, financial analysis, in particular, to assess the probability of default of non-lending organizations, to determine the reliability of commercial banks, to conduct sociological tests, and surveys, medical and biological research and other areas of public administration.

Keywords: higher educational institution, university, Webometric rating, Pade approximation, two-factor model.

**Introduction.** The Law of Ukraine "On Higher Education" (2014) states that state policy in the field of higher education is based on the principles of international integration and integration of the higher education system of Ukraine into the European Higher Education Area, provided that the preservation and development of the achievements and progressive traditions of the national higher education. In this context, the vector of modern trends in higher education in Ukraine is oriented towards the entry of the country into the educational and scientific space of Europe and the world, the modernization of educational activities in the context of the European canons, the development of programs for the modernization of

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the training of high-level specialists, competitive in the world labor market. The implementation of these areas will contribute to embedding global value chains (Koval et al., 2019). That is why the trend of recent years for advanced Ukrainian universities has been to analyze the results of their participation in significant international and national ratings.

Webometrics rating is one of the most well-known and authoritative academic ratings of higher education institutions. Since 2004, every six months, Spanish National Research Council (CSIC), Spanish National Research Council (Cybermetrics Lab) under the Ministry of Science and Innovation in Spain, conducts an independent, objective, free, and open-minded assessment of universities from all over the world to provide a reliable, multidimensional, updated and useful information about their work, based on the representation and influence in the Internet space (Ranking Web of Universities, 2019).

Webometric rating is estimated by more than 24 thousand universities of the world, including 323 Ukrainian, and published twice a year – in July and January. According to the authors, the Webometrix rating with the help of independent Web indicators and scientifically grounded model indirectly evaluates all aspects of the functioning of universities: scientific activity, educational work, development of culture, social status, sports achievements, and the very versatility distinguishes Webometrics from other Internet ratings. However, the most important in the rating are the figures of the citation of scientific publications of universities on the Internet and their representation in the database Scopus. The rating also positively takes into account the level of openness at the university, that is, the possibility of open access to the results of their scientific research, educational and methodological materials, normative base, etc.

Literature Review. The investigation of the quality factors of research and education activities of domestic higher educational institutions according to influential international ratings, as well as the analysis of evaluation indicators, are becoming more relevant in the context of European integration processes in Ukraine in modern times. This is due to the considerable interest of Ukrainian researchers in studying this problem. Thus, the work of Harvey (2008), Shin & Toutkoushian (2011), Westerheijden (2012), Porzionato & De Marco (2015), Kochetkova et al. (2016) are devoted to the analysis of modern ratings of Higher education as a tool for assessing the quality of higher education. In the article by Morze & Buinytska (2015), the issue of creating an open electronic environment as one of the most important tasks of universities in terms of improving the quality of education was considered. In the articles by Buinytska et al. (2013), Marginson, S. (2014) provides a comprehensive analysis of indicators of the Webometric rating and their impact on the generalized place of higher education in the ranking.

A generalized multidimensional correlation model of the dependence of the general rating of universities of Ukraine on the web indicators of Webometrics, based on the statistical material of the Webometric Ratings of Universities in January 2018, is presented in the work of Starushenko & Bazylevskyi (2018).

The publication of Novak et al. (2019) analyzed the correspondence of master's programs in higher educational institutions of the United States, the European Union and Ukraine, and based on the obtained results the recommendations were given regarding the modernization of master's programs in Ukraine up to standards of the European Higher Education Area. In the article by Nelipa & Batrymenko (2018), a strategy has been developed based on a competent approach, a management model is constructed, and an educational and scientific program of training civil servants in graduate school is presented. Rudenko et al. (2018) investigated in the scientific paper the peculiarities of the management of international educational projects between the universities of Poland and Ukraine, proposed to organize the management of international projects in the field of higher education and science through creation of independent management and financial aspects of joint educational and research centers, with the involvement of non-state scientific and educational organizations.

In the framework of the subject under consideration, it is expedient, in our opinion, to study the issue that was not yet adequately covered in the literature, namely, the construction of a two-factor model, which,

according to the Webometric rating, analytically describes at the time the representation of Ukrainian universities in the Internet space. Such a model will make it possible to calculate the forecast for the ranking of Ukrainian universities for Webometric indicators and will allow, if necessary, to correct the vector of scientific activity of domestic universities in order to improve the results of this or that Web indicator.

The objective of the article is the construction of the Webometric Rating of Universities of the two-factor model on the basis of the statistical material (Koval et al., 2018), which analytically describes the status of Ukrainian higher educational institutions in terms of Webometrics indicators, provides an opportunity for its quantitative and qualitative analysis and forecasting of development trends.

**Methodology and research.** The initial data for the construction of a two-factor model that describes the state, patterns and trends of the world ranking of Ukrainian universities in the Internet space by the Webometric Indicators system in time was a sample of 50 best-rated Ukrainian universities in the 2018-2019 period: in January 2018 (New Ranking Webometrics, 2018a), in July 2018 (New Ranking Webometrics, 2018b) and in January 2019 (Ranking Web of universities, 2019).

From the mathematical point of view, the construction of the desired model, illustrating the dependence of the ranking on two parameters – the place (number) of the university in the rating scale and the time parameter – leads to the need to construct the function of two variables:

$$z = z(y, t), \tag{1}$$

where y = y(x), x - a serial number of the university in the rating; t - t ime parameter.

Ukrainian universities that are part of the top 50 Ukrainian universities according to the Webometrix rating are re-coded according to the order (rank, ordinal scale), namely:  $x_i = i$ , i = 1, 2, ..., 50; with the higher serial number corresponding to the higher (worst) place of the university in the ranking.

The values of the time factor are determined as follows: t = 0 – January 2018; t = 6 – July 2018 and t = 12 – January 2019.

All statistical procedures used in constructing the model were performed in the program STATGRAPHICS Centurion XV.I.

**Results**. Using the STATGRAPHICS Simple Regression tool, we will construct the regressive dependence of the resultant attributes  $y_j$ , j = 1, 2, 3(the world ranking of Ukrainian universities in January 2018 – July 2018 – January 2019) from ordinary factors. The results of the calculations will be placed according to the table 1 – 3.

Summarizing conclusions based on the estimated data in Table 1-3 we will reduce in Table 4.

To write the expression of the desired function of the form (1), we use the Pade approximation method (Baker & Graves-Morris, 1996). If the function f(t) can be represented as a power series:

$$f(t) = \sum_{i=0}^{\infty} c_i t^i \tag{2}$$

then the Pade approximation is called the rational function of the form:

$$f_{[L/M]}(t) = \frac{a_0 + a_1 t + \dots + a_L t^L}{b_0 + b_1 t + \dots + b_M t^M}$$
(3)

the decomposition of which in a Maclaurin series coincides with expansion (5), as long as it is possible. The function of type (3) has L+1 coefficients in the numerator and M+1 – in denominator, and without limitation of the general nature of considerations can be put  $b_0=1$ .

Table 1. The regression model of the world ranking of Ukrainian universities in January 2018

# Simple Regression – World Rank January 2018 vs. Ukraine Rank January 2018

Dependent variable: World Rank January 2018 Independent variable: Ukraine Rank January 2018

Square root-X model: Y = a + b\*sqrt(X)

#### Coefficients

		-			
		Least Squares	Standard	T	
	Parameter	Estimate	Error	Statistic	P-Value
	Intercept	570.567	47.2868	12.0661	0.0000
	Slope	822.423	9.36418	87.8265	0.0000

**Analysis of Variance** 

Source	Sum of Squares	Df	Mean Square	F-Ratio	P-Value
Model	8.9443E7	1	8.9443E7	7713.50	0.0000
Residual	556591.	48	11595.6		
Total (Corr.)	8.99996E7	49			

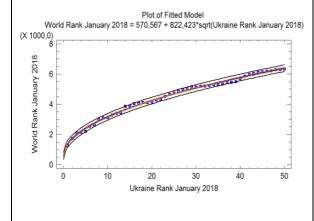
Correlation Coefficient = 0.996903 R-squared = 99.3816 percent

R-squared (adjusted for d.f.) = 99.3687 percent

Standard Error of Est. = 107.683 Mean absolute error = 87.9665

Durbin-Watson statistic = 0.753736 (P=0.0000)

Lag 1 residual autocorrelation = 0.606288



Comparison	of	Alternat	ive I	Models	

Model	Correlation	R-Squared
Square root-X	0.9969	99.38%
Multiplicative	0.9967	99.35%
Squared-Y	0.9958	99.16%
Double square root	0.9905	98.10%
Square root-Y logarithmic-X	0.9880	97.61%
Squared-Y square root-X	0.9854	97.10%
Linear	0.9767	95.39%
Logarithmic-Y square root-X	0.9720	94.48%
Logarithmic-X	0.9700	94.10%
Double squared	0.9582	91.81%
Square root-Y	0.9527	90.77%
Double reciprocal	0.9292	86.35%
Squared-Y logarithmic-X	0.9200	84.64%
Exponential	0.9162	83.94%
Squared-X	0.9025	81.45%
Square root-Y squared-X	0.8600	73.96%
S-curve model	-0.8188	67.05%
Logarithmic-Y squared-X	0.8062	65.00%
Reciprocal-Y	-0.8026	64.42%
Reciprocal-X	-0.6984	48.78%
Reciprocal-Y squared-X	-0.6676	44.57%
Squared-Y reciprocal-X	-0.5965	35.58%
Reciprocal-Y square root-X	<no fit=""></no>	
Reciprocal-Y logarithmic-X	<no fit=""></no>	
Square root-Y reciprocal-X	<no fit=""></no>	
Logistic	<no fit=""></no>	
Log probit	<no fit=""></no>	

Sources: compiled by authors.

Table 2. The regression model of the world ranking of Ukrainian universities in July 2018

#### Simple Regression - World Rank July 2018 **Comparison of Alternative Models** vs. Ukraine Rank July 2018 Model Correlation R-Squared Dependent variable: World Rank July 2018 Square root-X 0.9959 99.18% Independent variable: Ukraine Rank July 2018 Squared-Y 0.9955 99.10% Square root-X model: Y = a + b\*sqrt(X)Multiplicative 0.9936 98.73% Double square 0.9890 97.80% Coefficients root Least Squares Standard Squared-Y 0.9885 97.72% Parameter Estimate P-Value Error Statistic square root-X Square root-Y 0.9852 97.07% Intercept 516.728 52.3765 9.86565 0.0000 logarithmic-X 792.407 10.3721 0.0000 Slope 76.398 0.9733 94.74% Linear Logarithmic-Y 0.9724 94.56% **Analysis of Variance** square root-X F-Ratio P-Value Source Sum of Df Mean Logarithmic-X 0.9696 94.01% Squares Square Double 0.9518 90.59% 5836.65 0.0000 Model 8.30332E7 8.30332E7 1 squared Residual 682856. 48 14226.2 Square root-Y 0.9499 90.23% Total 8.37161E7 49 Squared-Y 0.9255 85.65% (Corr.) logarithmic-X Exponential 0.9165 83.99% Correlation Coefficient = 0.995913 Double 0.9055 82.00% R-squared = 99.1843 percent reciprocal 0.8940 R-squared (adjusted for d.f.) = 99.1673 percent Squared-X 79.93% Standard Error of Est. = 119.274 Square root-Y 0.8529 72.74% squared-X Mean absolute error = 87.7746 Reciprocal-Y -0.8183 66.97% Durbin-Watson statistic = 0.646155 (P=0.0000) Logarithmic-Y 0.8031 64.49% Lag 1 residual autocorrelation = 0.675805 squared-X S-curve model -0.8003 64.05% Plot of Fitted Model World Rank July 2018 = 516,728 + 792,407\*sqrt(Ukraine Rank July 2018) -0.6920 Reciprocal-X 47.89% (X 1000,0) Reciprocal-Y -0.6804 46.30% squared-X World Rank July 2018 -0.5994 35.92% Squared-Y reciprocal-X Reciprocal-Y <no fit> square root-X Reciprocal-Y <no fit> logarithmic-X Square root-Y <no fit> 30 40 reciprocal-X Ukraine Rank July 2018 \_ogistic <no fit> Log probit <no fit>

Sources: compiled by authors.

Table 3. The regression model of the world ranking of Ukrainian universities in January 2019

## Simple Regression – World Rank January 2019 vs. Ukraine Rank January 2019

Dependent variable: World Rank January 2019 Independent variable: Ukraine Rank January 2019

Multiplicative model:  $Y = a*X^b$ 

#### Coefficients

	Least Squares	Standard	T	
Parameter	Estimate	Error	Statistic	P-Value
Intercept	7.11314	0.0171756	414.141	0.0000
Slope	0.408916	0.00554542	73.7394	0.0000

NOTE: intercept = In(a)

#### **Analysis of Variance**

Source	Sum of	Df	Mean	F-Ratio	P-
	Squares		Square		Value
Model	6.47774	1	6.47774	5437.50	0.0000
Residual	0.0571829	48	0.00119131		
Total (Corr.)	6.53492	49			

Correlation Coefficient = 0.995615

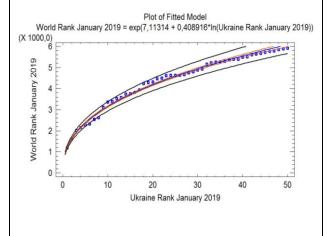
R-squared = 99.125 percent

R-squared (adjusted for d.f.) = 99.1067 percent

Standard Error of Est. = 0.0345154 Mean absolute error = 0.0260793

Durbin-Watson statistic = 0.627904 (P=0.0000)

Lag 1 residual autocorrelation = 0.672326



Comparison of Alternative Models	

Model	Correlation	R-Squared
Multiplicative	0.9956	99.12%
Squared-Y square root-X	0.9950	98.99%
Square root-Y logarithmic-X	0.9933	98.67%
Square root-X	0.9928	98.56%
Squared-Y	0.9900	98.00%
Logarithmic-X	0.9823	96.48%
Double square root	0.9799	96.02%
Linear	0.9585	91.87%
Logarithmic-Y square root-X	0.9559	91.37%
Squared-Y logarithmic-X	0.9455	89.40%
Double reciprocal	0.9429	88.90%
Double squared	0.9299	86.47%
Square root-Y	0.9293	86.36%
Exponential	0.8887	78.98%
Squared-X	0.8660	75.00%
S-curve model	-0.8415	70.82%
Square root-Y squared-X	0.8211	67.41%
Reciprocal-Y	-0.7714	59.50%
Logarithmic-Y squared-X	0.7662	58.71%
Reciprocal-X	-0.7294	53.20%
Squared-Y reciprocal-X	-0.6339	40.18%
Reciprocal-Y squared-X	-0.6301	39.70%
Reciprocal-Y square root-X	<no fit=""></no>	
Reciprocal-Y logarithmic-X	<no fit=""></no>	
Square root-Y reciprocal-X	<no fit=""></no>	
Logistic	<no fit=""></no>	
Log probit	<no fit=""></no>	

Sources: compiled by authors.

Table 4. Conclusions from the simple regression calculations

Table 4. Conclusions from the simple regression calculations						
January 2018	July 2018	January 2019				
Regression dependence of the world ranking of Ukrainian universities						
$y_1 = 570.567 + 822.423\sqrt{x}$ , (2) $y_2 = 516.728 + 792.407\sqrt{x}$ , (3) $y_3 = 1227.997x^{0.408916}$						
	Determination coefficient					
$R_l^2 = 99.3816$	$R_2^2 = 99.1843$	$R_3^2 = 99.125$				
shows that the models are explaine	d accordingly 99.3816%, 99.1843% effective factor	and 99.125% changes in the				
	Correlation coefficient					
$r_1 = 0.996903$	$r_2 = 0.995913$	$r_3 = 0.995615$				
defines for all n	nodels the strong interconnection of	variables				
	Standard error evaluation					
107.683 119.274 0.0345154						
defines the stan	dard deviation of the remnants for th	e models				
	Average absolute error					
87.9665	87.7746	0.0260793				
is th	ne average value of the remnants					
Col	mparison of alternative models					
	comparing the selected curvilinear re					
alternatives. Models (2) – (4) are the best in comparison with the alternatives by the coefficient of						
determination, beca	use the value of statistics $R^2$ in the	m is the most				
	Schedule					
, ,	t statistical data, regression curve, a	nd confidence intervals for				
baseline data and regression curves.						

Sources: compiled by authors.

Let's increase the expressions (1) - (2) by the variable t (time parameter) with the help of the three-point approximation of the Pade form:

$$z_{[0/2]}(t) = \frac{a_0}{1 + b_1 t + b_2 t^2} \tag{4}$$

where  $a_0$ ,  $b_i$ ,  $(i=1,\ 2)$  – constants on the variable t , which are determined from the conditions:

$$\frac{a_0}{1 + b_1 t + b_2 t^2} \bigg|_{t=0} = y_1;$$

$$\frac{a_0}{1 + b_1 t + b_2 t^2} \bigg|_{t=6} = y_2;$$

$$\left. \frac{a_0}{1 + b_1 t + b_2 t^2} \right|_{t=12} = y_3,$$

that is:

$$a_0 = 570.567 + 822.423\sqrt{x} \tag{5}$$

$$\frac{a_0}{1+6b_1+36b_2} = 516.728 + 792.407\sqrt{x} \tag{6}$$

$$a_0 = 570.567 + 822.423\sqrt{x}$$

$$\frac{a_0}{1+6b_1+36b_2} = 516.728 + 792.407\sqrt{x}$$

$$\frac{a_0}{1+12b_1+144b_2} = 1227.997x^{0.408916}$$
(7)

The solution of the system of equations (6), (7), obtained using the mathematical editor Maple, has the form:

$$b_1 = -\frac{{}^{44224.71052x - 76039.25x}{}^{0.9089159998} + 59520.38678\sqrt{x} - 61007x}{{}^{0.4089159998}(7.92407 \cdot 10^5\sqrt{x} + 5.16728 \cdot 10^5)} \tag{8}$$

$$b_2 = \frac{^{7370.785088x - 11839.43056x^{0.9089159998} + 9920.064463\sqrt{x} - 8672.305556x^{0.4089159998} + 3334.562354}{x^{0.4089159998} (7.92407 \cdot 10^5 \sqrt{x} + 5.16728 \cdot 10^5)}$$
 (9)

Consequently, taking into account (6), (8), (9), the world rating z Ukrainian Universities in the Internet Space by the System of Webometric Indicators, depending on the place of the university in the rating scale  $\mathcal{X}$  and time factor t is described by the analytical relation of the species:

$$z(x, t) = \frac{a_0}{1 + b_1 t + b_2 t^2},\tag{10}$$

Using the functions (5), (8), (9), (10) makes it possible: to obtain quantitative assessments and illustrate a qualitative picture of the rating of Ukrainian universities in the Internet space by Webometrix indicators during January 2018 - January 2019 (Fig. 1); to highlight the tendencies of the rating of domestic universities, showing its character in the forecast by July 2019 (Fig. 2). Charts in Figure 1 and Figure 2 are built in the mathematical editor Maple.

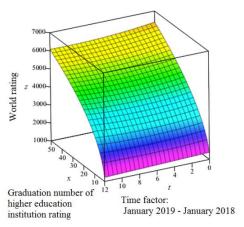


Figure 1. Webometric rating of Ukrainian universities in the period from January 2018 to January 2019 Sources: compiled by authors.

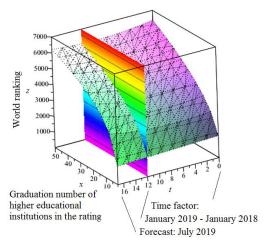


Figure 2. The rating of Ukrainian universities on the Webometric indexes from January 2018 by January 2019 and forecast by July 2019

Sources: compiled by authors.

The use of the relations (5), (8), (9), (10) obtained on the basis of the Pade approximation technique enables to calculate for the selected sample population the forecast of the average rating of Ukrainian universities in the Internet space in the Webometrix system of indicators.

For this we apply the expression (10), taking into account (5), (8), (9), the operator of averaging (Bakhvalov & Panasenko, 1989):

$$\tilde{z}(t) = \frac{1}{b-a} \int_{a}^{b} z(x,t) dx, \qquad (11)$$

and use the STATGRAPHICS Forecast tool to analyze the data. The results of calculation are given in Table. 5

For forcasting, the model of one-parameter linear exponential smoothing of Brown with (Table 5, Forecasting – Average Rank) is chosen. This model assumes that the best forecast for future data is determined by the linear trend, which is estimated by the exponential weight of all previous data values. According to error statistics (Table 5, Model Comparison) we find that the chosen model of one-parameter linear exponential smoothing of Brown (model E) is:

- Model with the lowest average square error (RMSE) during the assessment period;
- Model with the lowest average absolute error (MAE);
- Model with the lowest average absolute error (MAPE).

The selected *model E* passes 3 tests out of 5. Thus, according to the results of the analysis we find that the chosen one-parameter linear exponential smoothing model of Brown is the best among alternative models and can be used for prediction. The graph (Figure 3) is presented: source data for forecasting; graph of the function approximated by the model of one-parameter linear exponential smoothing of Brown; forecast of the average value of the world ranking of Ukrainian universities in the Internet space on the Webometrics system for 6 months (until July 2019 inclusive); Confidence intervals for the forecast at 95% confidence level.

### **Table 5. Calculation forecast**

Table 5. Calculation forecast							
Forecasting - Average Rank	recasting - Average Rank Model Comparison						
Data variable: Average Rank  Number of observations = 13  Start index = 1,0  Sampling interval = 1,0	Data variable: Average Rank Number of observations = 13; Start index = 1,0; Sampling interval = 1,0  Models  (A) Random walk with drift = -10,7901						
Forecast Summary Forecast model selected: Brown's linear exp. smoothing with alpha = 0,9999	(C) Sim (D) Sim (E) Bro	ear trend = nple movir nple expor wn's linea	ng averag nential sm r exp. sm	e of 3 tern oothing w	ns <sub>r</sub> ith alpha		
Number of forecasts generated:	Estima	tion Perio	od				
6	Model	RMSE	MAE	MAPE	ME		MPE
Number of periods withheld for	(A)	26,8341	22,1791	0,506561	3,7895	6E-13	0,00325043
validation: 0	(B)	49,8405	39,668	0,905677		06E-13	-0,0108669
	(C)	45,2436	38,2963	0,879943			-0,37576
Estimation Validation	(D)	27,8677	21,5015	0,490388			-0,225661
RMSE 22,922	(E)	22,922	14,5935	0,329708	-1,794	4	-0,035388
MAE 14,5935	Model	RMSE	RUNS	RUNM	AUTO	MEAN	VAR
MAPE 0,329708	(A)	26,8341	***	**	*	***	OK
ME -1,7944	(B)	49,8405	***	*	*	OK	OK
MPE -0,035388	(C)	45,2436	***	*	OK	*	OK
2   0,000000	(D)	27,8677	***	*	OK	**	OK
	(E)	22,922	**	OK	OK	OK	***
The table below shows:  RMSE – mean square error;  MAE – average absolute percentage error;  ME – mean error;  MPE is the average percentage error.  The first three statistics measure the magnitude of errors, and the best model gives it less value.  The last two statistics measure displacement; the best model gives it a value close to 0.  Key:  RMSE = Root Mean Squared Error  RUNS = Test for excessive runs above and below mediance.  AUTO = Box-Pierce test for excessive autocorrelation.  MEAN = Test for difference in variance 1st half to 2nd half on the open of the					n lalf half  asting models. carried out on consideration  which is a strong models.		

level of 99.9%.

#### Continued Table 5

The table below shows:

RMSE – mean square error;

MAE – average absolute error;

MAPE – average absolute

percentage error;

ME - mean error;

MPE is the average percentage error.

The first three statistics measure the magnitude of errors, and the best model gives it less value. The last two statistics measure displacement; the best model gives it a value close to 0.

The table compares the results of five different forecasting models. The table also contains the results of the five tests carried out on the residue to determine whether each model under consideration is adequate to the statistical data:

OK means that the model passes the test;

- \* means that the model does not pass the test at 95% confidence level;
- \*\* means that the model does not pass the 99% trust test;
- \*\*\* mean that the model does not pass the test at the confidence level of 99.9%.

Sources: compiled by authors.

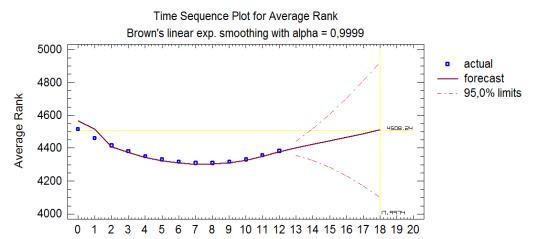


Figure 3. The forecast of the average world rating of the top 50 Ukrainian universities in the internet space for 6 months under the indicator system Webometrics

Sources: compiled by authors.

Thus, according to forecasted calculations at 95% confidence level, the average value of the world ranking of the top 50 Ukrainian universities in the Internet space by indicators of Webometrics in July 2019 will slightly deteriorate compared with January 2019 and will be approximately  $\hat{z}=4508\pm400$ , that is, it will be in the range: $4108 \leq \hat{z} \leq 4908$ .

**Conclusions**. On the basis of the statistical material of the Webometric rating of the top 50 Ukrainian universities during January 2018 – January 2019, a two-factor model that analytically describes the status of Ukrainian higher education institutions in terms of Webometrics, has been constructed, enables quantitative and qualitative analysis and forecasting of development trends. Statistical processing and analysis of the Webometric Ratings of Universities was conducted using the Professional Statistical Information Processing Program STATGRAPHICS Centurion XV.I. The analysis of regression and

predictive models and comparisons with alternative models is based on their adequacy to statistical data and acceptability for practical use.

Analytical relations on the model were obtained using the Pade approximation technique. Mathematical editor Maple has been used to perform mathematical transformations as well as visualize the results of research and illustrate a qualitative picture of the rating of Ukrainian universities in the Internet space using the Webometric indicators system. The proposed method of constructing a model can be extended to a larger sample of statistical material and a more significant time interval: its algorithm in this case will not undergo fundamental changes and complications. The presented methodology and data analysis algorithm allow for a generalization of the evaluation of rating systems of other nature: when assessing the educational and public work of students, in financial analysis, in conducting sociological tests and surveys, in medical biology studies and in other areas of public administration.

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Маркетинг представленості українських закладів вищої освіти на основі моделювання рейтингів у Вебометрікс Метою статті є побудова на основі статистичного матеріалу Вебометричного рейтингу університетів двофакторної моделі, яка аналітично описує у часі стан українських вищих навчальних закладів за показниками Вебометрікс, що дає можливість його кількісного й якісного аналізу та прогнозування тенденцій розвитку ринку освітніх послуг та маркетингових досліджень у цій сфері. Статистичний аналіз даних Вебометричного рейтингу університетів проведено із застосуванням професійної програми статистичної обробки інформації STATGRAPHICS Centurion XV.I. Аналітичні співвідношення отримані за допомогою техніки Паде-апроксимацій. Для візуалізації результатів дослідження та ілюстрації якісної картини рейтингу українських ВНЗ в Інтернет-просторі за системою Вебометричних індикаторів використано математичний редактор Марle. Побудовано двофакторну модель стану і прогнозу академічної представленості українських університетів за даними Вебометричного рейтингу. Із застосуванням пропонованої моделі отримано аналітичний вираз, що дає змогу кількісної й якісної оцінок світового рейтингу вищих навчальних закладів України в системі Веб-індикаторів Вебометрікс щодо збільшення їх академічної присутності в Інтернеті, зміцнення міжнародного авторитету і підняття в цілому вітчизняної наукової школи на якісну нову ступінь розвитку. Наукова новизна роботи полягає у включенні в модель часового чинника, наявність якого дає можливість, по-перше, розширювати у часі використовуваний статистичний матеріал і, по-друге, прогнозувати тенденції і перспективи представлення в Інтернет-просторі університетів України як передових науково-дослідницьких центрів. Основні результати роботи можуть бути корисними в якості методичного матеріалу при проведенні учбового процесу у вищих навчальних закладах, при навчанні і підвищенні кваліфікації управлінських кадрів, при розробці програм реформування освітнього процесу у вищій школі з метою наближення його до європейського вимог і досягнення рівня найкращих світових університетів. Представлена методика й алгоритм аналізу даних можуть бути узагальнені для оцінки рейтингових систем іншої природи: при оцінюванні навчальної та громадської роботи учнів і студентів, у фінансовій аналітиці, зокрема, для оцінки ймовірності дефолту некредитних організацій, при визначенні надійності комерційних банків, при проведенні соціологічних тестів і опитувань, в медико-біологічних дослідженнях та в інших сферах публічного vnравління.

Ключові слова: заклад вищої освіти, університет, вебометричний рейтинг, апроксимація Паде, двухфакторная модель.

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